

describe how close are the reliability evolution paths of each software instance. This may reveal hidden topological similarities between software products and help us to characterise its reliability behaviour. In this preliminary study we illustrated the idea how we can use topological data analysis for that purpose that give us some promising results that is motivation for our future work.

In future work we want to compare obtained distances between projects to the traditional reliability growth models [14, 16, 13]. From this future work we expect to gain deeper understanding of different reliability behaviour among software products and relate it to theory of reliability growth modelling. This knowledge may be useful in early characterisation of software system reliability behaviour that can lead to early determination of the best reliability growth modeling approach. As we show from analysed examples of software systems this approach may be very useful to provide a measure of development environment with respect to various system properties. This information may be very useful in early determination of the best mathematical model for system behaviour.

The choice of distance used to construct the simplicial complexes that originate the persistence diagrams can have influence on the information extracted from them. This is a topic of discussion in further work, where we shall also study in depth the interpretation of the information provided by the persistence diagram in the context of the original problem.

Moreover, the study of the dynamics of the reliability evolution itself, and the identification of patterns, can be accessed by these methods and will also be subject of further research. Also the distinctions between the different levels of persistence landscapes can complement the comparison information provided, and thus contribute to this research.

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